## Working Group 2 Dependence Modelling and Elicitation

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## MAIN ACHIEVEMENTS

#### > STSM

- > WG2 meeting
- > Published systematic literature reviews
  - Research progress on process and biases
  - Subject expert opinions to empirical control
  - > Graph specification for BNs



## SHORT TERM SCIENTIFIC MISSIONS

- Christoph Werner (Strathclyde) July 2014.
- Maria Nogal (Trinity College Dublin)
   March 2016
- Alex Kosgodagan (École des Mines de Nantes) October 2016
- > Sophia Wright (Warwick) 2017
- > A number of publications
  - > Published/in press
  - Accepted
  - Submitted
  - Collaboration still going on





A 2-dimension dynamic Bayesian network for large-scale degradation modelling with an application to a bridges network

Computer-Aided Civil and Infrastructure Engineering

Computer-Aided Civil and Infrastructure Engineering



Impact Factor: 5.786 ISI Journal Citation Reports © Ranking: 2016: 1/61 (Construction & Building Technology); 1/34 (Transportation Science & Technology); 2/125 (Engineering Civil); 3/105 (Computer Science Interdisciplinary Applications)

Online ISSN: 1467-8667

Edited By: Hojjat Adeli





BATIONAL CLEMAN

## WG2 MEETING WARSAW JUNE 2016

- Christoph Werner (Scotland)
- Maria Nogal (Ireland)
- Daniel Puig (Denmark)
- Grzegorz Król (Poland)
- Simona Miraglia (Denmark)
- Fabrizio Ruggeri (Italy)
- Oswaldo Morales Napoles (Netherlands)









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## "DEPENDENCE CALIBRATION"

- Paper(s) submitted
- 1 recent MSc thesis used both methods
- 1 application in resilience of traffic networks
- 1 application (precipitation) assessing asymetries bivariate distributions

Understanding the vulnerability of traffic networks by means of structured expert judgment Calibration and Combination of Experts' Dependence Estimates





#### ASCE-ASME Journal of Risk and Uncertainty in Engineering Systems, Part A: Civil Engineering

ISSN (online): 2376-7642 Frequency: Quarterly | Sponsored by the Committee on Technical Advancement

#### Characterization of Precipitation through Copulas and Expert Judgement for Risk Assessment of Infrastructure

Oswaldo Morales-Nápoles<sup>1</sup>; Dominik Paprotny<sup>2</sup>; Daniël Worm<sup>3</sup>; Linda Abspoel-Bukman<sup>4</sup>; and Wim Courage<sup>5</sup>

Abstract: In this paper two methodologies are investigated that contribute to better assessment of risks related to extreme rainfall events.



### OVERVIEW OF CONSIDERATIONS ALONG EJ PROCESS WHEN ELICITING DEPENDENCE

Book chapter in press (Springer International Series in OR and MS)

Werner C, et al., Eliciting Multivariate Uncertainty from Experts: Considerations and Approaches along the Expert Judgement Process. (Chapter 8)"

Contains:

- Literature review on cognitive fallacies when eliciting dependence
- Overview of dependence elicitation process



International Textus in Operations Research and Research Concer

International Series in Operations Research And Management Science



### REVIEW ON DEPENDENCE ELICITATION



CrossMari

Published article (EJOR)

Contains:

- Expert judgement methods for various common dependence models (in different modelling contexts)
- Review of commonly elicited forms and their assessment burden



#### Invited Review

Expert judgement for dependence in probabilistic modelling: A systematic literature review and future research directions

Christoph Werner  $^{a_a},$  Tim Bedford  $^a,$  Roger M. Cooke  $^b,$  Anca M. Hanea  $^c,$  Oswaldo Morales-Nápoles  $^d$ 

Department of Management Science, University of Struthclyde, Giargow, United Kingdom
 Brosources for the Future, Washington, DC, USA
 Centre of Excellance for Biosciencity Risk Analysia, University of Melbourne, Melbourne, Australia
 Faculty of Civil Engineering and Geosciences, Delt University of Technology, Delt, The Netherlands



## Bias mitigation & structuring experts' knowledge on dependence: Mapping conditional scenarios



- 1 Paper under review
- 1 application in higher education risk assessment (managing portfolio of income streams in HE)
- Further applications planned, e.g. in antibacterial resistance risk assessment
- Extended abstract won Donald Hicks Scholarship from UK OR Society (for presenting at EURO 2016)



7/13/2017

Mapping Conditional Scenarios for Knowledge Structuring in

(Tail) Dependence Elicitation



University of Strathcly

Business

Detailed and feasible assessment of dependence through *sequential refined conditioning* 

7/13/2017



### UNDERSTANDING THE VULNERABILITY OF TRAFFIC NETWORKS BY MEANS OF STRUCTURED EXPERT JUDGMENT ELICITATION

Maria Nogal

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#### Intro

#### Motivation

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#### Questions Postprocess

Formulation

Modelling Copulas Dependence modelling Example

Analysis of results

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Conclusion





#### **Example: Questionnaire**

Intro

Motivation

Structure Expert

Elicitation

Experts

Questions

Postprocess

Cooke method

Formulation

Analysis of results

Dependence Modelling

Copulas

Dependence modelling

Example

Conclusions



#### Descriptor:

Intrinsic vulnerability,  $V_{i,j}$ : susceptibility to incidents characterised by their random occurrence in space and time that can result in considerable reduction or loss of the functionality.

#### Indicators:

Reliability  $(R_{i,j})$  & accessibility  $(A_{i,j})$ .

Calibration Variables		Variables of Interest (percentile 50)										
Galibration Variables		ODs	$Prob(V_{i,j} A_{i,j})$	$Prob(V_{i,j} A_{i,j},R_{i,j})$								
$Prob(A_{25,69} A_{32,92})$	0.499	20-25										
$Prob(A_{32,92} A_{69,92})$	0.455	25-69										
$Prob(A_{25,69} A_{32,92},A_{69,92})$	0.500	32-69	-69 Unknown values									
$Prob(R_{25,69} R_{32,92})$	0.575	32-92										
$Prob(R_{32,92} R_{69,92})$	0.871	69-92										
$Prob(R_{25,69} R_{32,92},R_{69,92})$	0.563											

#### **Results & discussion**

Introduction

RAIN

Context

Resilience

Goal How

Structured expert judgmer

What is it?

Mathematical foundation

Proof of Concept

Intrinsic vulnerability

Results

Conclusions



- Reliability and accessibility are both valid indicators to assess the intrinsic vulnerability of the network.
- Other indicators are required to explain a high percentage of the vulnerability.
- The most vulnerable ODs can be identified.

TRINITY COLLEGE DUBLIN

Nogal, M., Morales-Napoles, O. and O'Connor, A. Understanding the vulnerability of traffic networks by means of structured expert judgment elicitation (submitted).

## STRUCTURAL ELICITATION FOR BAYESIAN NETWORKS

- STSM of Sophia Wright (Warwick University), together with Tina Nane (TU Delft) and Anca Hanea (Cebra, Melbourne University), November 2016 and February 2017
- Learning the structure of a BN
  - Need for a performance-based elicitation protocol
  - How can we measure performance when eliciting the structure of a BN?
- Setting citation analysis
  - Data citation performance of Canadian researchers
  - Experts 5 experts in citation analysis from CWTS, Leiden University



## STRUCTURAL ELICITATION FOR BAYESIAN NETWORKS

- The approach
  - Expert
    - 1. Ask experts about conditional distribution of the variables of interest (IDEA protocol implemented with two rounds of Classical Model)
  - Data
    - 2. Assign arcs in a particular order
    - 3. Compute the conditional distribution of the variables of interest
    - 4. Repeat 2&3
  - Compare the conditional distributions in 1 and 3
  - Choose the conditional distribution from the data closest to the conditional distribution from experts (with respect to a particular distance)

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## STRUCTURAL ELICITATION FOR BAYESIAN NETWORKS

- Conclusions
  - Regardless the arcs assignment, the conditional distribution of the variables of interest might not change
  - Given a particular structure of the BN, the experts can assess conditional distributions of the variables of interest quite accurately
  - IDEA can help experts to become better calibrated
  - IDEA can increase the performance of the DM



Motivating problem SHeffield ELicitation Framework (SHELF) Vines as prior distributions Example Summary

# The SHeffield ELicitation Framework and vine copulas in the specification of prior distributions for multinomial models

#### Kevin Wilson

School of Mathematics and Statistics, Newcastle University, UK Thanks to Lesley Walls, John Quigley, University of Strathclyde

#### 4th July 2017

Motivating problem SHeffield ELicitation Framework (SHELF) Vines as prior distributions Example Summary



- A group of engineers are responsible for a large road bridge.
- The bridge is coming to the end of its useful life.
- The engineers would like to assess the condition of the bridge.

- Typical approaches to eliciting priors for multinomial distributions restrict the possible dependence structures.
- Vines can give a more flexible dependence specification, with the same number of expert specifications.
- D-vines represent a suitable vine structure and parametric copulas contain the flexibility for the required dependency.
- The elicitation can be expressed in terms of quantities about which we could ask an expert.

## REFLECTION

- Good Progress
  - > As evidenced by previous slides
  - > In good measure thanks to the COST Action
- Still much to do
  - Process
  - > Theory
  - > Applications

